

# Swelling of Poly(methyl methacrylate-co-poly(oxytetramethylene) dimethacrylate)s

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**ABSTRACT:** Swelling studies are given for copolymers of methyl methacrylate (MMA) with poly(oxytetramethylene) dimethacrylate (POTMDM). An equation applicable to the swelling equilibrium of cross-linked copolymer + solvent ternary systems is presented, which includes an assumption that the ratio between the different elastic expansion factors,  $\alpha_1$  and  $\alpha_2$ , is constant at various compositions. This equation is applicable to the swelling behavior for poly(MMA-co-POTMDM) with various ( $M_1/M_2$ ), though the negative  $\chi_{12}$  values are estimated for the copolymer in moderately hydrogen-bonded solvents. These extraordinary  $\chi_{12}$  values are explained in terms of a contribution of hydrogen bonding to the enthalpy.

## Introduction

Copolymers of methyl methacrylate (MMA) with poly(oxytetramethylene) dimethacrylate (POTMDM) have either a MMA polymer (PMMA) chain or a poly(oxytetramethylene) (POTM) chain between cross-links, and, therefore, some of their physical and physicochemical properties are considered to be influenced by the MMA/POTM composition. Actually, even a POTMDM homopolymer exhibits a dependence of the relaxation process on the methacrylate/oxytetramethylene composition of the polymer.<sup>1,2</sup>

The Flory-Rehner equation<sup>3,4</sup> is used for interpreting consistently the swelling behavior of cross-linked polymer + solvent binary systems.<sup>5-7</sup> However, the Flory-Rehner equation with the number-average molecular weights of polymer chains of PMMA and POTM overestimates the degree of swelling of poly(MMA-co-POTMDM).

The expression for the cross-linked copolymer + solvent ternary systems should include two different polymer-solvent interaction parameters,  $\chi_{01}$  and  $\chi_{02}$ , and a polymer-polymer interaction parameter,  $\chi_{12}$ , and two different expansion factors,  $\alpha_1$  and  $\alpha_2$ , for PMMA and for POTM.

In the present work, our object is to derive and evaluate an equation applicable to the swelling equilibrium of poly(MMA-co-POTMDM) + solvent systems. The derivation of the swelling entropy is carried out according to a swelling cycle provided by Flory.<sup>4</sup> Here the most difficult problem is to differentiate the elastic expansion factors,  $\alpha_1$  and  $\alpha_2$  with respect to the number of solvent molecules,  $n_0$ . Assuming that  $\alpha_1/\alpha_2$  is independent of  $n_0$ , we derive an equation of swelling equilibrium for poly(MMA-co-POTMDM) + solvent ternary systems.

The copolymers studied here span the MMA/POTM composition range 1/3 to 400/1 (w/w).

## Experimental Section

**Poly(oxytetramethylene) Dimethacrylate (POTMDM).** The synthesis of POTMDM was performed by an usual esterification procedure<sup>8</sup> using poly(oxytetramethylene) (POTM) with two hydroxy end groups and an excess of fresh methacryloyl chloride (10 times the stoichiometric amount). The reaction mixture was poured into warm water (about 330 K). The product was yielded after phasing out, washed with warm water several times, and dried at room temperature under vacuum. The fresh methacryloyl chloride was readily prepared, following a general procedure<sup>9</sup> starting with benzoyl chloride and methacrylic acid

(both reagents were purchased from Wako Pure Chemicals USA, Ltd., Dallas, TX). By a courtesy of du Pont Japan Ltd., poly(oxytetramethylene) glycol (teratane 2900,  $M_n \approx 2900$ ) was provided to the present work.

**Polymerization.** All polymers used in the present work were prepared by bulk polymerization at 333 K for 24 h in a flame-sealed 20-mm  $\phi$  glass tube. Benzoyl peroxide (Wako Pure Chemicals USA, Ltd.) recrystallized twice from ethanol was used as an initiator. We chose 10 MMA/POTMDM weight ratios in feed, in the range 1/3 to 400/1 (w/w), in order to obtain the copolymers with different MMA compositions. After Soxhlet extraction with acetone, the residual copolymer was dried under vacuum until its weight became constant. The PMMA content in copolymer was determined by weighing the polymer after the extraction, since the most abundant product extracted was linear PMMA. Methyl methacrylate (Wako Pure Chemicals USA, Ltd.) was used after distillation under reduced pressure.

A copolymer of MMA with 0.1 wt % of ethylene dimethacrylate (EDMA) was synthesized by a similar bulk polymerization, for determination of the polymer-solvent interaction parameter of PMMA.

**Swelling Experiment.** A ca. 20 mm  $\phi \times$  ca. 5 mm disk of polymer precisely weighed was immersed in a solvent at 298 K for 4 days. The swollen polymer was surface-dried and weighed in a closed vessel. The resulting volume fraction,  $v_p$ , of polymer in the swollen polymer was given as

$$v_p = [d_p d_0^{-1} (s_w - 1) + 1]^{-1}$$

where  $d_p$  and  $d_0$  are the densities of polymer and solvent and  $s_w$  is the weight degree of swelling obtained as the ratio of weights between starting and swollen polymers. The  $d_p$  values were obtained by weighing polymer in atmosphere and in ethanol.

All solvents used in the swelling experiment were purchased from Wako Pure Chemicals USA, Ltd., and were purified by usual methods.<sup>10</sup>

## Partial Molal Free Energy of Swelling

**Entropy of Swelling.** The entropy of swelling may be calculated by using the entropy changes associated with the following processes:<sup>3,4</sup> (1) interlinking of undiluted polymer chains ( $\Delta S_1$ ), (2) dilution of polymer chains with solvent molecules ( $\Delta S_2$ ), (3) interlinking of diluted polymer chains ( $\Delta S_3$ ), and (4) swelling of the polymer network ( $\Delta S_4$ ):

$$\Delta S_s = \Delta S_2 + \Delta S_3 - \Delta S_1 \quad (1)$$

The MMA/POTMDM copolymer is the assemblage of  $n_1$  PMMA chains and  $n_2$  POTM chains. The probability

of formation of network,  $\Omega_1$ , is given by

$$\Omega_1 = \omega_1 \omega_2 \quad (2)$$

where  $\omega_1$  and  $\omega_2$  are the probabilities of formation of a chain end surrounded by two PMMA chains and by a PMMA chain and a POTM chain. The probability that a chain end in an element with a volume of  $\Delta\tau$  will be surrounded by a polymer chain is equal to the product of the number of chains and  $\Delta\tau/V$  where  $V$  is the volume of the whole swollen network. Therefore,  $\omega_1$  and  $\omega_2$  are given by (Appendix)

$$\omega_1^{1/2} = 3^{(n_2+1)} (\Delta\tau/V)^{(n_2+1)} (2n_1/3)! / [(n_2-1)/3]!$$

$$\omega_2 = \omega_{21} \omega_{22}$$

$$\omega_{21} = (\Delta\tau/V)^{n_2} (n_1-1)! / (n_2-1)!$$

$$\omega_{22} = 3^{n_2} (\Delta\tau/V)^{n_2} [(4n_2+1)/3-1]! / [(n_2+1)/3]!$$

Introducing the Stirling approximation and using the Boltzmann relation, we may express the entropy change through process 1 as

$$\Delta S_1 = (4/3)kn \ln (4n\Delta\tau/3Ve) + (2/3)kn \ln 2 \quad (3)$$

where  $n = n_1 + n_2$  and  $n_1 = 2n_2$  are used, and  $k$  is the Boltzmann constant and  $e$  is the Napier number.

The entropy of mixing through process 2 may be in accordance with the expression applied to a mixture of two polymers with different chain lengths and a solvent<sup>11-13</sup>

$$\Delta S_2 = -k(n_0 \ln v_0 + n_1 \ln v_1 + n_2 \ln v_2) \quad (4)$$

where  $n_0$  is the number of solvent molecules and  $v_0, v_1$ , and  $v_2$  are the volume fractions of solvent molecule 0, PMMA chain 1, and POTM chain 2.

Process 3 is accomplished by dilation of the most probable chain displacement length distribution by the factors  $\alpha_1$  for PMMA chain and  $\alpha_2$  for POTM chain, followed by joining of the dilated chains. Assuming that PMMA and POTM chains are independently dilated and according to the derivation<sup>3,4,7</sup> for binary systems, we give the elastic entropy,  $\Delta S_{el}$ , for ternary systems as

$$\Delta S_{el} = kn_1(\ln \alpha_1^3 - (3/2)\alpha_1^2 + 3/2) + kn_2(\ln \alpha_2^3 - (3/2)\alpha_2^2 + 3/2) \quad (5)$$

The joining is accomplished in a fashion analogous to process 1. Then  $\Delta S_3$  is given by

$$\Delta S_3 = (4/3)kn \ln (4n\Delta\tau v_p/3Ve) + (2/3)kn \ln 2 + \Delta S_{el} \quad (6)$$

where  $v_p$  is the volume fraction of polymer; i.e.,  $v_p = v_1 + v_2$ .

Finally, substituting these various expressions in eq 1, we obtain

$$\Delta S_s = -k(n_0 \ln v_0 + n_1 \ln v_1 + n_2 \ln v_2) + k(n_1 \ln \alpha_1^3 + n_2 \ln \alpha_2^3) - (3/2)k(n_1 \alpha_1^2 + n_2 \alpha_2^2 - n_1 - n_2) + (4/3)kn \ln v_p \quad (7)$$

In order to obtain the partial molal entropy of swelling with respect to solvent by using eq 7,  $v_1$  and  $v_2$  are replaced by  $n_1 Z_1 / (n_0 + n_1 Z_1 + n_2 Z_2)$  and  $n_2 Z_2 / (n_0 + n_1 Z_1 + n_2 Z_2)$ , where  $Z_1$  and  $Z_2$  represent the ratios of the volume of a PMMA chain and a POTM chain to the volume of solvent, and  $Z_1$  and  $Z_2$  are approximately replaced by  $M_1/d_1 V_0$  and  $M_2/d_2 V_0$ , where  $d_1$  and  $d_2$  are the densities of MMA homopolymer and POTM (practically POTMDM) homopolymer and  $V_0$  is the molar volume of solvent. Now we need

**Table I**  
Values of  $\delta_0^a$  and  $\chi_{01}$  for the Solvents Studied

solvent	$10^{-3}\delta_0/\text{J}^{1/2} \text{ m}^{-3/2}$	$\chi_{01}$
toluene	18.2	0.436
tetrahydrofuran (THF)	18.6	0.348
benzene	18.8	0.423
1,2-dichloroethane (DCE)	20.1	0.379
p-dioxane	20.5	0.393
N,N-dimethylacetamide (DMA)	22.1	0.385
N-methyl-2-pyrrolidone (NMP)	23.1	0.354
N,N-dimethylformamide (DMF)	24.8	0.448

<sup>a</sup>  $\delta_0$  in ref 23.

to express  $\alpha_1$  and  $\alpha_2$  as a function of  $n_0$ . For a swollen copolymer, the length,  $X$ , to the direction of the  $x$ -axis is given as the sum of  $X_1$  and  $X_2$ , where  $X_1$  and  $X_2$  are the sums of the lengths to the direction of the  $x$ -axis for PMMA and POTM chains. The length,  $X'$ , to the direction of the  $x$ -axis for the starting copolymer, is given as the sum of  $X_1/\alpha_1$  and  $X_2/\alpha_2$ . Assuming that  $X'$  is proportionally distributed to  $X_1/\alpha_1$  and  $X_2/\alpha_2$  with respect to the numbers of bond vectors, we obtain

$$X_1/\alpha_1 = wX'/(w+1) \quad (8)$$

$$X_2/\alpha_2 = X'/(w+1) \quad (9)$$

where  $w$  is the ratio of the weight of PMMA chain to the weight of POTM chain and is equal to  $n_1 M_1 / n_2 M_2$ . Since  $X/X'$  is equal to  $v_p^{-1/3}$ , we can obtain the relation

$$w\alpha_1/(w+1) + \alpha_2/(w+1) = v_p^{-1/3} \quad (10)$$

Furthermore, we may have another relation between  $\alpha_1$  and  $\alpha_2$  as

$$\alpha_1/\alpha_2 = r \quad (11)$$

where  $r$  is independent of  $n_0$ . By combination of eqs 10 and 11,  $\alpha_1$  and  $\alpha_2$  are replaced by  $v_p^{-1/3}rg$  and  $v_p^{-1/3}g$ , where  $g = (1+w)/(1+rw)$ . Thus we differentiate eq 7 with respect to  $n_0$  and thereby obtain the partial molal entropy of swelling:

$$\Delta \bar{S}_s = -R[\ln(1-v_p) + v_p - (2/3)(v_1/Z_1 + v_2/Z_2) + v_p^{-2/3}(v_1 r^2 g^2/Z_1 + v_2 g^2/Z_2)] \quad (12)$$

**$\chi$  Function.** There are various expressions of the thermodynamic interaction parameter  $\chi$  for polymer + polymer + solvent ternary systems.<sup>14-17</sup> Some of them are very complicated and inadequate to interpret, our experimental results involving many parameters. Here we use the simple and certain expression<sup>17</sup>

$$\chi v_p^2 = \chi_{01} v_1^2 + \chi_{12} v_1 v_2 + \chi_{02} v_2^2 \quad (13)$$

where  $\chi_{01}$  and  $\chi_{02}$  denote the  $\chi$  functions for the binary systems of PMMA + solvent and POTM + solvent, and  $\chi_{12}$  is the  $\chi$  function between PMMA and POTM in the ternary system. Accordingly, the partial molal free energy of swelling is given by

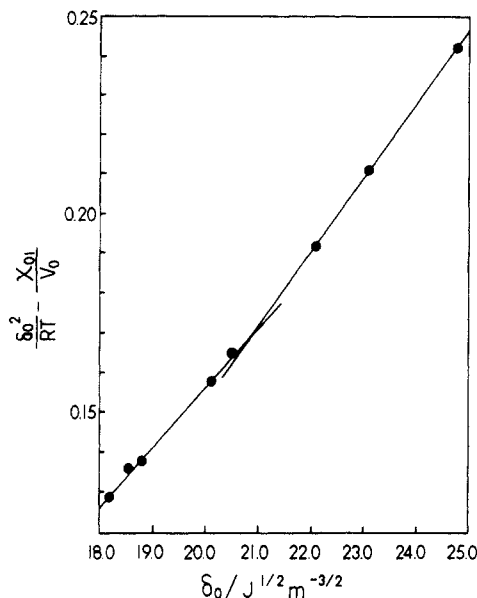
$$\Delta \bar{G}_s = RT(\chi_{01} v_1^2 + \chi_{12} v_1 v_2 + \chi_{02} v_2^2) - T\Delta \bar{S}_s \quad (14)$$

Thus in the swelling equilibrium of cross-linked copolymers

$$\chi_{01} v_1^2 + \chi_{12} v_1 v_2 + \chi_{02} v_2^2 + \ln(1-v_p) + v_p - (2/3)(v_1/Z_1 + v_2/Z_2) + v_p^{-2/3}(v_1 r^2 g^2/Z_1 + v_2 g^2/Z_2) = 0 \quad (15)$$

## Results and Discussion

**Determination of  $\chi_{01}$ .** The  $\chi_{01}$  values for various solvents in Table I were determined from the swelling data



**Figure 1.** Bristow-Watson plot for poly(MMA-co-EDMA) with 0.1 wt % of EDMA. The straight lines were obtained by the least-squares method.

of poly(MMA-co-EDMA) with a small amount of EDMA (0.1 wt % of EDMA), according to the Flory-Rehner expression<sup>3,4</sup>

$$\ln(1 - v_p) + v_p + \chi_{01}v_p^2 = -(d_1V_0/M_1)(v_p^{1/3} - 2v_p/f) \quad (16)$$

where  $f$  is the functionality of cross-link ( $f = 4$  for the poly(MMA-co-EDMA)),  $v_p$  is close to the volume fraction of PMMA, and  $M_1/M_{EDMA}$  is almost equal to a half of the MMA/EDMA weight ratio in the copolymer, where  $M_{EDMA} = 198$ . Using the  $\chi_{01}$  values for various solvents in Table I, we made a plot of  $\delta_0^2/RT - \chi_{01}/V_0$  versus  $\delta_0$ , which had been proposed by Bristow and Watson,<sup>7</sup> in order to evaluate the solubility parameter according to the usual expression<sup>18-20</sup>

$$\chi_{0i} = \chi_{is} + V_0(\delta_0 - \delta_i)^2/RT \quad (17)$$

where  $\delta_0$  and  $\delta_i$  are the solubility parameters of solvent and polymer  $i$  and  $\chi_{is}$  is the constant concerning the coordination number and the chain length of polymer. The Bristow-Watson plot in Figure 1 seems to exhibit two slopes. Values of  $\delta_1/J^{1/2} m^{-3/2}$  equal to 19.1 from the slope and 19.4 from the intercept of the plot for  $\delta_0$  from 18.0 to 21.0  $J^{1/2} m^{-3/2}$  and 22.9 from the slope and 23.1 from the intercept of the plot for  $\delta_0 > 21.0 J^{1/2} m^{-3/2}$  were obtained for poly(MMA-co-EDMA) with 0.1 wt % of EDMA. The  $\delta_1$  values are fairly close to  $\delta_1 = 18.9 J^{1/2} m^{-3/2}$  calculated from the structural formula by using the group molar attraction constants.<sup>21-23</sup>

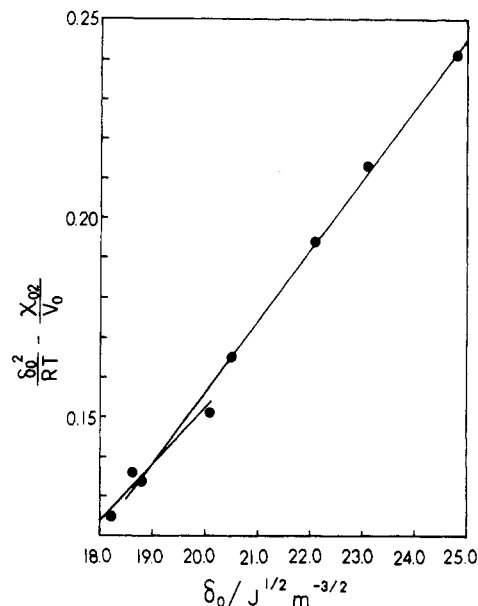
**Determination of  $r$ .** By using eq 15 with a large  $w$  value ( $w = 200$  or  $300$ ), where  $\chi_{02}v_2^2$  and  $\chi_{12}v_1v_2$  are negligible, we were determined the  $r$  values for various solvents, where  $v_1$  and  $v_2$  were replaced by  $d_2wv_p/(d_1 + d_2w)$  and  $d_1v_p/(d_1 + d_2w)$ . The  $r$  values in Table II are in a narrow range of 0.20–0.35 and seem to be independent of the solubility parameter of the solvent.

**Determination of  $\chi_{02}$ .** For the POTMDM homopolymer,  $w (=2M_1/M_2)$  is equal to  $9.485 \times 10^{-3}$ , where  $M_1$  is given as the molecular weight of  $CH_2$  and  $M_2$  is the sum of the molecular weights of two C=O and POTM used in the present work, and therefore  $\chi_{12}v_1v_2$  and  $\chi_{01}v_1^2$  are negligible in eq 15. Thus we can obtain the  $\chi_{02}$  values by application of eq 17 to the homopolymer.

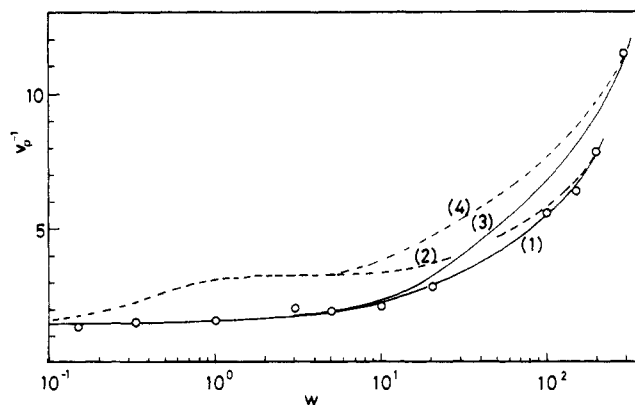
**Table II**  
Values of  $r$ ,  $\chi_{02}$ , and  $\chi_{12}$  for the Solvents Studied

solvent	$r$		$\chi_{02}$		$\chi_{12}^c$
	$w = 200$	$w = 300$	$r_{200}^a$	$r_{300}^b$	
toluene	0.25	0.32	1.045	1.040	2.16
THF	0.21	0.26	0.435	0.414	-1.41
benzene	0.27	0.31	0.890	0.886	2.84
DCE	0.27	0.29	0.985	0.983	0.95
<i>p</i> -dioxane	0.30	0.35	0.492	0.472	-0.53
DMA	0.27	0.30	0.407	0.392	-0.62
NMP	0.24	0.26	0.340	0.330	-2.50
DMF	0.20	0.24	0.598	0.590	-0.80

<sup>a</sup>  $\chi_{02}$  obtained by use of  $r$  at  $w = 200$ . <sup>b</sup>  $\chi_{02}$  obtained by use of  $r$  at  $w = 300$ . <sup>c</sup>  $\chi_{12}$  obtained by use of  $r$  at  $w = 200$ .



**Figure 2.** Bristow-Watson plot for poly(POTMDM). The straight lines were obtained by the least-squares method.



**Figure 3.** Representative relations between  $v_p^{-1}$  and  $w$  for the copolymers in toluene used as a poorly hydrogen-bonded solvent: (1)  $r = 0.25$ ,  $\chi_{01} = 0.436$ ,  $\chi_{02} = 1.045$ , and  $\chi_{12} = 2.16$ ; (2)  $r = 0.25$ ,  $\chi_{01} = 0.436$ ,  $\chi_{02} = 1.045$ , and  $\chi_{12} = 0.00$ ; (3)  $r = 0.32$ ,  $\chi_{01} = 0.436$ ,  $\chi_{02} = 1.045$ , and  $\chi_{12} = 2.16$ ; (4)  $r = 0.32$ ,  $\chi_{01} = 0.436$ ,  $\chi_{02} = 1.045$ , and  $\chi_{12} = 0.00$ .

The Bristow-Watson plot depicted by using the  $\chi_{02}$  values exhibits also two slopes, as shown in Figure 2. Values of  $\delta_2/J^{1/2} m^{-3/2}$  are equal to 17.8 from the slope and 18.6 from the intercept of the plot for  $\delta_0$  from 18.0 to 21.0  $J^{1/2} m^{-3/2}$  and 21.5 from the slope and 21.8 from the intercept for  $\delta_0 > 21.0 J^{1/2} m^{-3/2}$ . The former  $\delta_2$  are in accord with  $\delta_2$  equal to 17.8  $J^{1/2} m^{-3/2}$ , calculated from the structural formula.

**Determination of  $\chi_{12}$ .** Now we have experimentally known  $\chi_{01}$ ,  $\chi_{02}$ ,  $v_1$ ,  $v_2$ ,  $Z_1$ ,  $Z_2$ , and  $r$  in eq 15, and therefore we can obtain the  $\chi_{12}$  values by application of eq 15 to the copolymers with various  $w$  values. The  $\chi_{12}$  values in Table II are the mean of the  $\chi_{12}$  values at  $w = 1, 3$ , and 5. Depending on whether the  $\chi_{12}$  value is positive or negative, the solvents are classified into two distinct groups A and B: A, toluene, benzene, and DCE; B, THF, dioxane, DMA, NMP, and DMF. The solvents of groups A and B are known as poorly hydrogen-bonded solvents and moderately hydrogen-bonded solvents,<sup>23</sup> respectively.

Figures 3 and 4 show representative relations between  $v_p^{-1}$  and  $w$  for the copolymers in toluene and DMA, respectively. Curve 1 in Figure 3 and curve 4 in Figure 4 are in good accord with observed relations between  $v_p^{-1}$  and  $w$ . Similar results were obtained for the copolymers in other solvents. The negative  $\chi_{12}$  values for the copolymers in a moderately hydrogen-bonded solvent suggest the existence of association caused by a solvent-polymer hydrogen bond, since  $\chi_{12}$  should be inherently positive and independent of the solubility parameter of solvents. Accordingly, for moderately hydrogen-bonded solvents, eq 15 is modified as

$$\chi_{01}v_1^2 + \chi_{12}v_1v_2 + \chi_{02}v_2^2 + \frac{\Delta\bar{H}_H}{RT} - \frac{\Delta\bar{S}_s}{R} = 0 \quad (18)$$

where  $\Delta\bar{H}_H$  is the partial molal enthalpy of hydrogen bonding and is negative. Roughly estimated,  $\Delta\bar{H}_H$  values are in the range of 6–9 kJ mol<sup>-1</sup>, which is close to the enthalpy of hydrogen bond formation in the literature.<sup>24,25</sup>

### Appendix: Derivation of $\Delta S_1$

We consider formation of a network in a way in which  $\omega_1$  and  $\omega_2$  are given as

$$\omega_1 = [2n_1(\Delta\tau/V)]^2[(2n_1-3)(\Delta\tau/V)]^2[(2n_1-6)(\Delta\tau/V)]^2 \dots [n_2(\Delta\tau/V)]^2$$

$$\omega_2 = [(2n_2-1)(\Delta\tau/V)(2n_1-2)(\Delta\tau/V)][(2n_2-2)(\Delta\tau/V)(2n_1-5)(\Delta\tau/V)] \dots = \omega_{21}\omega_{22}$$

$$\omega_{21} = [(2n_2-1)(\Delta\tau/V)][(2n_2-2)(\Delta\tau/V)] \dots [n_2(\Delta\tau/V)]$$

$$\omega_{22} = [(2n_1-2)(\Delta\tau/V)][(2n_1-5)(\Delta\tau/V)] \dots [(n_2+1)(\Delta\tau/V)]$$

These equations are replaced by factorial expressions as follows:

$$\omega_1^{1/2} = 3^{(n_2+1)}(\Delta\tau/V)^{(n_2+1)}(2n_1/3)!/[(n_2-1)/3]!$$

$$\omega_{21} = (\Delta\tau/V)^{n_2}(n_1-1)!/(n_2-1)!$$

$$\omega_{22} = 3^{n_2}(\Delta\tau/V)^{n_2}[(4n_2+1)/3-1]!/[(n_2+1)/3]!$$

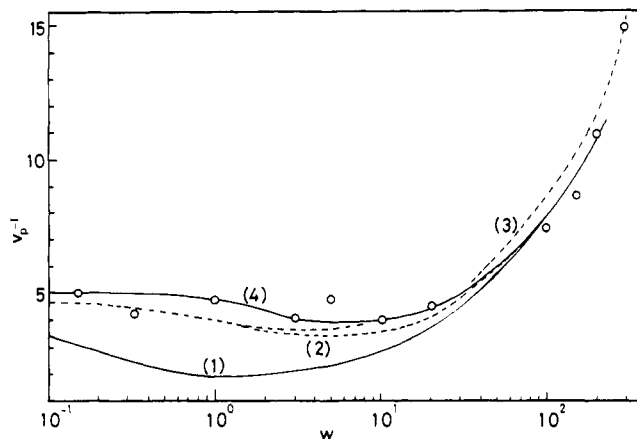
Using the Stirling approximation, we obtain the logarithms of  $\omega_1$ ,  $\omega_{21}$ , and  $\omega_{22}$  as

$$\ln \omega_1 = 2n_2 \ln (\Delta\tau/V) + (4n_1/3) \ln 2n_1 - (2n_2/3) \ln n_2 - 2n_2$$

$$\ln \omega_{21} = n_2 \ln (\Delta\tau/V) + n_1 \ln n_1 - n_2 \ln n_2 - n_2$$

$$\ln \omega_{22} = n_2 \ln (\Delta\tau/V) + (2n_1/3) \ln (2n_1) - (n_2/3) \ln n_2 - n_2$$

where  $n_1 = 2n_2$  and  $n_2 \gg 1$ .



**Figure 4.** Representative relations between  $v_p^{-1}$  and  $w$  for the copolymers in DMA used as a moderately hydrogen-bonded solvent: (1)  $r = 0.27$ ,  $\chi_{01} = 0.385$ ,  $\chi_{02} = 0.407$ , and  $\chi_{12} = 2.5$ ; (2)  $r = 0.27$ ,  $\chi_{01} = 0.385$ ,  $\chi_{02} = 0.407$ , and  $\chi_{12} = 0.0$ ; (3)  $r = 0.30$ ,  $\chi_{01} = 0.385$ ,  $\chi_{02} = 0.407$ , and  $\chi_{12} = 0.0$ ; (4)  $r = 0.27$ ,  $\chi_{01} = 0.385$ ,  $\chi_{02} = 0.407$ , and  $\chi_{12} = -0.62$ .

Accordingly, using the Boltzmann relation, we obtain the  $\Delta S_1$  expression, i.e., eq 3:

$$\Delta S_1 = k \ln (\omega_1 \omega_2) = (4/3)kn \ln (4n\Delta\tau/3Ve) + (2/3)kn \ln 2$$

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**Registry No.** (MMA)(POTMDM) (copolymer), 52277-34-6; EDMA, 25777-71-3; THF, 109-99-9; DCE, 107-06-2; DMA, 127-19-5; NMP, 30207-69-3; DMF, 68-12-2; toluene, 108-88-3; benzene, 71-43-2; p-dioxane, 123-91-1.